

# History, current developments, and future directions of near-field optical science

M. Ohtsu

Research Origin for Dressed Photon,  
3-13-19 Moriya-cho, Kanagawa-ku, Yokohama, Kanagawa 221-0022, Japan

## Abstract

This paper reviews the science of the optical near-field (ONF), which is created and localized in a nanometer-sized material (NM) or on its surface. It is pointed out that work on near-field optics was started in order to break through the diffraction limit in optical microscopy and had already come to an end without giving answers to the essential questions on the origin of the near-field optical interaction. However, recent studies have reincarnated these studies and identified the ONF as an off-shell quantum field. Based on this identification, a novel science called off-shell science has started on the basis that the dispersion relation between energy and momentum is invalid for the ONF. This quantum field is called the dressed photon because it is created as a result of the interaction between photons and electrons (or excitons) in a NM and, thus, it accompanies the energies of electrons or excitons. In reviewing current developments, this paper presents fifteen novel phenomena that are contrary to the common views in conventional optical science. Novel technologies developed by applying these phenomena are also reviewed. These include: nanometer-sized optical devices, nano-fabrication technology, and energy conversion technology. High-power Si light emitting diodes, Si lasers, and SiC polarization rotators are reviewed as examples of electrical to optical energy conversion. For future directions, this paper also reviews novel theoretical studies that have commenced recently by relying on physical and mathematical bases.

## 1 Introduction

The relatively new optical science of dressed photons (DPs) has seen rapid progress recently. The DP is a quantum field created in a complex system composed of photons and electrons (or excitons) in a nanometer-sized material. The fruits of this science have been applied to develop generic technologies (for example, nanometer-sized optical devices, information processing systems using these devices, nano-fabrication technology, and energy conversion technology) to realize disruptive innovations. Furthermore, studies on off-shell science have commenced. Off-shell science is a novel optical science

including studies on the DP. The origin of this science can be found in near-field optics, which was actively investigated in the 1980s and 1990s after a long period of incubation since the 1920s. Studies on near-field optics started with the aim of achieving disruptive innovations in optical science, especially in optical microscopy. Although extensive studies were carried out in the 1980s and 1990s, they have mostly already come to an end. However, basic studies exploring the nature of the optical near field (ONF) were steadily continued by a small number of scientists, and near-field optics was reincarnated as a novel science of the DP. This science involves the study of light-matter interactions in a nanometer-sized space and explores novel applications that are contrary to those in conventional optical science and technology.

The author of this paper (M.O.) has been engaged in work on near-field optics for over three decades, spurred by a simple and intuitive desire to miniaturize the dimensions of light [1,2]. He pioneered DP science based on the long-term accumulation of his studies. Since the circumstances at the end and subsequent reincarnation of near-field optics mentioned above may not be widely known, especially by the young scientists, this paper starts by reviewing the history of near-field optics in Section 2. Next, current developments in studies on the DP are reviewed in Section 3. Possible directions for the future are suggested in Section 4. Section 5 summarizes the paper.

## **2 History**

To start a review on the history of near-field optics, first, the principles of creating and detecting the ONF should be explained: Scattered light is created when a nanometer-sized material (NM1) is illuminated by light. It should be noted that another form of electromagnetic field is also created in NM1 or on its surface. This field is called the ONF. The ONF is localized on NM1, and its spatial extent (size) is equivalent to the size of NM1. The ONF cannot be detected by a conventional photodetector installed far from NM1 because it does not propagate to the far field. To detect it, a second nanometer-sized material (NM2) is inserted into the ONF. The ONF is disturbed by NM2 and is converted to scattered light that propagates to the far field, and is thus detected by a photodetector.

Since the size of the ONF is equivalent to the size of NM1, it is expected that one can use the ONF to break through the diffraction limit which determines the spatial resolution in optical microscopy. In such a system, the ONF on NM1 works as a light source for acquiring an optical microscope image of NM2. Based on this expectation, research on near-field optics was started with the aim of realizing this breakthrough, and a great deal of effort was made to create an ONF whose size  $\Delta x$  is much smaller than

the wavelength  $\lambda$  of light ( $\Delta x \ll \lambda$ ).

Since conventional optical theories were used in the early studies on near-field optics, the momentum  $p$  of the electromagnetic field has been treated as a definite quantity even though it is accompanied by a small uncertainty  $\Delta p$  due to quantum fluctuations. However, it should be pointed out that Heisenberg's uncertainty principle  $\Delta p \cdot \Delta x \geq \hbar$  ( $\hbar = h / 2\pi$ , where  $h$  is Planck's constant) indicates a large uncertainty  $\Delta p$  ( $\Delta p \gg p$ ) because of the relation  $\Delta x \ll \lambda$  above.

As will be reviewed in Section 3, modern studies are treating the ONF as a quantum field with a large energy uncertainty  $\Delta E$  as well as a large  $\Delta p$ . In particular, by examining the light-matter interactions in nanometer-sized spaces, a variety of novel phenomena that are contrary to those in conventional optical phenomena have been discovered. That is to say, near-field optics was reincarnated as a novel optical science, and the ONF was renamed the DP. Taking note of this reincarnation, the history of near-field optics is reviewed in the following.

It has been recognized that the classical period of near-field optics started in the 1920s to 1950s, with proposals that it be applied to high-resolution optical microscopy to achieve resolutions beyond the diffraction limit [3-5]. Diffraction and radiation of the electromagnetic field from a small aperture were analyzed based on classical electromagnetic field theory [6,7]. Instead of using NM1 mentioned above, a small aperture was used for experimental demonstrations in the microwave frequency region [8].

In the 1980s and 1990s, experimental demonstrations in the optical frequency region were finally made by several scientists around the world, including the author of this paper (M.O.). These include a method of acquiring an optical microscope image of sub-wavelength sized materials by scanning an aperture or a probe. The equipment assembled for this imaging was named an ONF microscope, a scanning near-field optical microscope, or a near-field scanning optical microscope [9]. It was used for acquiring high-resolution images beyond the diffraction limit [10-13]. In the early stages of these studies, since the performance of the aperture or probe was not sufficiently high, it was not straightforward to acquire sufficiently high-resolution images. However, the advent of high-quality fiber probes enabled high-resolution imaging and quantitative analysis of the acquired images [14]. High-precision technology for fabricating and using high-quality fiber probes propelled the development of ONF microscopy, allowing it to join the family of scanning tunneling microscopy (STM) [15-20]. In parallel with these experimental studies, the ONF microscopes mentioned above were used to acquire images of chemical and biological specimens [21-23] and to analyze the optical properties

of materials [24,25]. These microscopes are now commercially available [26]. Evaluation of the spatial resolution of such microscopes [27], spectral analysis of the ONF [28], and a proposal for a self-consistent theory including many body effects [29] have also been made.

For promoting studies on near-field optics, a compact international workshop was held in 1992 [9]. Theoretical pictures of the ONF were drawn in this workshop based on the conventional optical method using the dispersion relation between the momentum and energy of light. Based on future outlooks for near-field optics in a panel discussion at this workshop chaired by the author (M.O.), an international near-field optics conference was organized, which is periodically held even now. To promote studies also in the Asia-Pacific region, the author (M.O.) organized the Asia-Pacific near-field optics workshop in 1996 [30]. After this workshop, the Asia-Pacific near-field optics conference was organized and is still periodically held.

In the studies above, since the ONF and relevant phenomena have been discussed in the framework of conventional wave-optics, the electromagnetic origin of the ONF, and especially the origin of the light-matter interactions in nanometer-sized space, have remained unrevealed. However, a salvation was that quantum theoretical studies were started as a first step in revealing the nature of these interactions [31, 32].

Although near-field optics had succeeded in breaking through the diffraction limit by the 1990s, a technical problem was that the data acquisition time was too long because the fiber probe had to be slowly scanned under precise feedback servo-control. Furthermore, since other members of the STM family (such as atomic force microscopes and scanning electron tunneling microscopes) had already realized spatial resolutions as high as or higher than that of ONF microscopes, it was not straightforward to make the prominent performance of ONF microscopes appealing to nonprofessional users. A more essential problem was that the image-acquiring process in an ONF microscope disturbed the electron energies in the specimen. This is because the image is acquired by using the near-field optical interaction between the tip of the fiber probe and the specimen. In other words, NM1 (the tip of the fiber probe) and NM2 (the specimen) are not independent of each other but are combined via the near-field optical interaction. Thus, even though a high spatial resolution beyond the diffraction limit was realized, the problem was that the profile of the acquired image did not have a direct correlation with that of a conventional optical microscopic image. On the whole, the classical studies of the ONF in the 1980s and 1990s did not give any clear answers to the essential questions, “What is the origin of the near-field optical interaction?” and “What kind of optical scientific revolution could near-field optics have made?” By recognizing that these questions had been

neglected, the application of the ONF to microscopy, i.e., the study of near-field optics in the classical period, effectively came to an end.

However, even after this end, basic studies on the concepts and principles of the ONF were steadily continued by a small number of scientists. In relation to these studies, experiments on controlling atomic motion with high spatial resolution were carried out in a high vacuum [33]. Thanks to these continuous studies, a modern period of studies has started via transient studies named nano-optics or nanophotonics [34,35]. As a result, novel optical science and technology, based on the DP, have emerged as the reincarnation of classical near-field optics. These will be reviewed in the next section.

### **3 Current developments**

From the current studies of the DP as the reincarnation of classical near-field optics, novel phenomena that are contrary to those accepted in conventional optical science have been found. This section presents these phenomena and their applications to novel technologies.

#### **3.1 A name change: optical near field to dressed photon**

In order to review the current developments in studies on the DP, five common views that have been accepted for a long time in conventional optical science are listed here: [a] Light is a propagating wave that fills a space. Its spatial extent (size) is much larger than its wavelength. [b] Light cannot be used for imaging and fabrication of sub-wavelength sized materials. Furthermore, it cannot be used for assembling and operating sub-wavelength sized optical devices. [c] For optical excitation of an electron, the photon energy must be equal to or higher than the energy difference between the relevant two electronic energy levels. [d] An electron cannot be optically excited if the transition between the two electronic energy levels is electric-dipole forbidden. [e] Crystalline silicon has a very low light emission efficiency, and thus, it is unsuitable for use as an active medium for light emitting devices.

The origin of these common views is attributed to the dispersion relation of the photon, which definitely fixes the relation between energy  $E$  and momentum  $p$ . In the case where light propagates in a vacuum, the dispersion relation is linear ( $E=cp$ , where  $c$  is the speed of light). By noting that momentum is a three-dimensional vector, this relation is geometrically represented by a circular cone. In the case of propagation in a material, this relation is geometrically represented by a paraboloid. This circular cone and paraboloid have been called the mass-shell, and thus, propagating light is considered to

be an electromagnetic field in the on-shell state (“on-shell field” for short) because it is on the mass-shell. Even though the quantum fluctuations of the light have to be taken into account, conventional optical science has treated light in the on-shell state. Thus, this science can be called on-shell science. The common views [a]-[e] above are for light in the on-shell state, and they have become accepted in on-shell science.

Contrary to propagating light in the on-shell state described above, the ONF is in the off-shell state, which deviates from the circular cone and the paraboloid above. This is because its sub-wavelength size  $\Delta x$  ( $\ll \lambda$ ), being contrary to the common view [a] above, produces a large momentum uncertainty  $\Delta p$  ( $\Delta p \gg p$ ) due to the Heisenberg’s uncertainty principle  $\Delta p \cdot \Delta x \geq \hbar$ , as was described in Section 2.

Since  $p$  and  $E$  are mutually dependent, the electromagnetic field in the off-shell state (“off-shell field” for short) also has a large uncertainty  $\Delta E$  ( $\gg E$ ) in the energy. Thus, Heisenberg’s uncertainty principle ( $\Delta E \cdot \Delta t \geq \hbar$ ) also gives  $\Delta t \ll \hbar / E$ . This indicates the short duration of the field, which corresponds to the nature of a virtual photon. Due to the two large uncertainties ( $\Delta p$  and  $\Delta E$ ), the science of the ONF belongs to the category of off-shell science [36]. It should be noted that the natures of on-shell and off-shell fields are contrary to each other. The off-shell field is created neither in a vacuum nor in a super-wavelength sized macroscopic material. Instead, this field exhibits the following phenomenon: [*Phenomenon 1*] *The off-shell field is created and localized on a sub-wavelength material.*

Since this field is created as a result of the interactions between photons and electrons (or excitons) in an NM, it is the electromagnetic field that accompanies the electronic or excitonic energy. Thus, this field has been named the DP [36]. In other words, the DP is the quantum field created in a complex system composed of photons and electrons (or excitons) in an NM. It has a sub-wavelength size and short duration. By using the DP, novel phenomena (including *Phenomenon 1* above) that are contrary not only to the common view [a] but also to common views [b] – [e] have been found. Disruptive innovations in application technologies have been realized by applying these phenomena; and these technologies are presented in this section.

Theoretical studies have been carried out to draw the following two physical pictures of the DP:

#### 1) Creation and annihilation of the DP

Creation and annihilation operators are required to describe the energy exchange during light-matter interactions. In the case of the DP, however, the problem was that the DP has a sub-wavelength size. This meant that one could not define a virtual cavity, and thus, could not define the mode of the field for deriving its Hamiltonian. As an urgent solution

to this problem, the conventional theories of quantum optics were modified and applied to express photons of sub-wavelength size as a superposition of an infinite number of modes that interacted with the excitons of infinite energy levels in the NM [36]. As a result, creation and annihilation operators of the DP were derived, which were expressed by the sum of the operators of the photon of an infinite number of electromagnetic modes and those of the exciton of an infinite number of energy levels. This means that the photon "dressed" the exciton energy, and thus, this quantum field was named the DP [36]. It should be noted that this summation and dressing results in a broadband spectrum of the created DP even if a narrow-spectrum single-mode photon is incident on the NM.

As an example of further dressing of the material energy, coupling between the DP and phonon has been found: After a DP is created on an atom in a crystal under light illumination, it hops to the adjacent atom and excites a crystal-lattice vibration, creating phonons. The DP couples with these phonons and accompanies their energies. The creation and annihilation operators of this coupled state were expressed as the product of the DP operators above and the displacement operator of multi-mode phonons [37], which indicated that the DP couples with the multi-mode coherent phonons.

## 2) Spatial localization of the DP

In order to detect the DP that is created and localized on NM1, the DP must be converted to propagating scattered light, as was described at the beginning of Section 2. This can be performed by inserting NM2 into the DP field. Propagating scattered light is created by this insertion, and it reaches a photodetector in the far-field where it is detected. Although NM1 and NM2 may be considered as a light source and a detector in this process, one should note the following two phenomena that have been briefly described in the latter half of Section 2. The first one is *[Phenomenon 2] The DP energy transfers back and forth between the two NMs*. Due to this transfer, the light source and detector above are not independent of each other but are coupled in the nanometer-sized space, and thus, they cannot be distinguished as individual elements. The second one is *[Phenomenon 3] The DP field is conspicuously disturbed and demolished by inserting NM2 for detection*.

By noting these two phenomena, spatial localization of the DP has been studied for a system composed of two NMs between which the DP energy is transferred [31,38]. This study assumed that a nanometer-sized subsystem (composed of two NMs and the DP) was buried in a macroscopic subsystem (composed of a macroscopic host material, incident light, and scattered light). Since the light-matter interaction in the nanometer-

sized subsystem is the main subject of the study, the effects originating from the surrounding macroscopic subsystem were renormalized by the projection operator method.

By assuming also that the exciton-polariton in the macroscopic subsystem follows a paraboloidal dispersion relation, the magnitude of the effective interaction energy between the two NMs, mediated by the localized DP, was derived. It was represented by a Yukawa function whose spatial extent corresponded to the size of the NM. This indicates that the size of the DP corresponded to that of the NM. Although this spatial localization feature has been empirically known from experimental studies on the ONF, it was successfully formulated by the renormalization above. Furthermore, the following phenomenon was also formulated [38]: *[Phenomenon 4] The efficiency of the DP energy transfer between two NMs is highest when the sizes of the NMs are equal.* This phenomenon was named size-dependent resonance, and is nothing more than the momentum-conservation law for the DP energy transfer.

Although the long-wavelength approximation has been popularly used in conventional optical scientific studies on light-matter interactions, they are invalid in the case of the DP because its spatial extent, derived above, is much shorter than the wavelength of light. Due to this invalidity, a phenomenon that is contrary to the common view [d] was found: *[Phenomenon 5] An electric-dipole forbidden transition is allowed in off-shell science.*

The two physical pictures above have been actively used to propel experimental studies on the DP by using semiconductor NMs, organic NMs, and gaseous molecules. The light-matter interactions involving these specimens were analyzed by considering the discrete energy levels of the electrons or the excitons in the materials. By applying the results of these studies, novel technologies have been developed to bring about disruptive innovations, as will be reviewed in Section 3.2.

In comparison with the studies above, extensive studies have been carried out using metallic NMs or films, resulting in the realization of a novel technology named plasmonics, which uses the interaction between light and the plasmonic oscillation of free electrons in a metal [39]. This technology employs light-scattering phenomena that occur by controlling the dispersion relation of the polariton-plasmon. Since the collective motion of the electrons in metals is involved in this phenomena, optical energy is converted promptly to plasma oscillation energy. Furthermore, since the phase-relaxation



time of the electrons is very short, the unique properties of light, such as its quantum properties, are promptly lost in the metal. Therefore, to analyze the plasmonic phenomena, it is sufficient to use conventional wave-optical quantities, such as refractive index, wave-number, guiding mode, and the dispersion relation. In other words, these analyses are still based on wave optics, i.e., on-shell science.

### **3.2 Application to novel technologies**

Even though the theoretical studies carried out so far were for the purpose of finding an urgent solution to the problems noted above, they have ingeniously contributed to the realization of innovative generic technologies, including novel nanometer-sized optical devices, nano-fabrication technology, and energy-conversion technology. Among them, this section reviews a few examples and presents novel phenomena that originate from the intrinsic nature of the DP and are contrary to the common views [a]–[e] in Section 3.1

#### **3.2.1 Nanometer-sized optical devices and their applications**

This section reviews novel nanometer-sized optical functional devices, named DP devices, developed by using semiconductor NMs. They have enabled the transmission and readout of optical signals by DP energy transfer and subsequent dissipation. The operation of the DP devices was analyzed by using a quantum mechanical master equation based on a density matrix formulation [40]. Practical NOT logic gate and AND logic gate devices that operated at room temperature have been fabricated by using InAs NMs [41]. One advantage of these devices was that their extremely small sizes (20–50 nm side length in the case of the logic gate devices using InAs NMs) were far beyond the diffraction limit, contrary to the common view [b]. Other advantages were their superior performance levels and unique functionality, such as single-photon operation [42], extremely low energy consumption [43], and autonomous energy transfer [44]. These advantages originated from the unique operating principles of DP devices achieved by exploiting *Phenomena 4* and *5* in Section 3.1. Furthermore, a phenomenon inherent to off-shell science was used for the device operation: [*Phenomenon 6*] *The DP energy transfers among NMs autonomously.*

Novel information processing systems have been proposed by using DP devices [45]. The first example is a non-Von Neumann computing system utilizing DP energy

transfer. The ability to solve a decision making problem [46] and an intractable computational problem [47] has been demonstrated. The second example is an information security system that uses *Phenomenon 4* in Section 3.1. This system has realized a lock-and-key [48]. Furthermore, a hierarchical hologram [49] has been developed using the following phenomenon that originates from the size-dependent resonance (*Phenomenon 4*): [*Phenomenon 7*] *The DP energy transfer exhibits hierarchical features.*

### 3.2.2 Nano-fabrication technology

This section starts by reviewing an example of nano-fabrication technology that uses a fiber probe or an aperture. The specific natures of the DP relevant to this technology, and that are contrary to the common view [b] in Section 3.1, are also demonstrated. Next, a more practical technology is reviewed, in which neither the fiber probe nor aperture is required.

#### (1) Technology using a fiber probe or an aperture

This part reviews photochemical vapor deposition (PCVD) based on a DP–molecule interaction, as an example in which a fiber probe is used. It involves molecular dissociation by the DP and subsequent deposition of the dissociated atoms on a substrate.

$\text{Zn}(\text{C}_2\text{H}_5)_2$  (“DEZn” for short) was adopted as a specimen molecule. A DP was created on the tip of the fiber probe by irradiating the end of the fiber probe with light. Gaseous DEZn molecules, filled in a vacuum chamber, dissociated when these molecules jumped into the DP field. Here, the tip of the fiber probe and the molecule correspond to NM1 and NM2 in Section 2, respectively. The dissociated Zn atom subsequently landed on the substrate. After a short migration on the substrate, the Zn atom was adsorbed on the substrate. By repeating these dissociation and deposition processes, the number of adsorbed Zn atoms increased, resulting in the deposition of Zn atoms and the formation of a nanometer-sized metallic Zn-NM on the substrate.

For comparison, in the case of dissociating the DEZn molecules by using conventional propagating light, the wavelength was required to be shorter than 270 nm (photon energy 4.59 eV) for exciting an electron in the DEZn molecule (refer to the common view [c]). By noting this requirement, the following ingenious contrivances (i)-(iii) were employed in order to confirm that the DEZn molecules were dissociated only

by the DP in the PCVD above.

(i) The wavelength of the propagating light for creating the DP was set longer than 270 nm, contrary to the common view [c]. As a result, it was expected that the DEZn molecules would not be dissociated even if they were irradiated with the propagating light that leaked out from the tip of the fiber probe into the vacuum. Instead, it was expected that the DEZn molecules would be dissociated only by the DP on the tip due to the following phenomenon: [*Phenomenon 8*] The photon energy  $h\nu$  can be lower than the excitation energy of the electron  $E_{ex} - E_g$ , where  $E_{ex}$  and  $E_g$  are the energies of the excited and ground states of the electron, respectively. That is, since the created DP is the quantum field accompanying the energies of the excitons ( $E_{exciton}$ ) and phonons ( $E_{phonon}$ ) at the tip of the fiber probe, its energy is expressed as  $h\nu_{DP} = h\nu + E_{exciton} + E_{phonon}$ . Thus, even though  $h\nu < E_{ex} - E_g$ , the DP energy  $h\nu_{DP}$  can be larger than  $E_{ex} - E_g$  ( $h\nu_{DP} \geq E_{ex} - E_g$ ), which enables the dissociation of DEZn molecules [50].

(ii) In order to insure that the contribution of the propagating light was excluded (refer to (i)), an unreliable fiber probe was used to intentionally cause the propagating light to leak out from the taper and tip of the fiber probe into the vacuum. That is, the fiber probe used here was fabricated by heating and mechanically pulling the fiber to form a sharp tip. This was a very primitive method in comparison with the high-precision and highly reproducible selective etching method [14, 16]. Thus, high-precision control of the size, cone angle, and throughput were not expected. In addition, the probe was not coated with a metallic film, allowing the propagating light to leak out.

(iii) For further insurance, the DEZn molecules were replaced by zinc-bis(acetylacetonate) (“Zn(acac)<sub>2</sub>” for short) molecules [51]. Zn(acac)<sub>2</sub> is a well-known optically inactive molecule that has never been shown to be dissociated by propagating light. However, it was expected, from *Phenomenon 5*, that it could be dissociated by the DP.

Figures 1(a) and (b) show images of a Zn-NM formed on a sapphire substrate by dissociating DEZn molecules; these images were acquired by using an atomic force microscope (AFM) [50]. The wavelengths of the propagating light for creating the DP were as long as 488 and 684 nm, respectively, which indicate that the contribution from the propagating light was excluded due to contrivances (i) and (ii) above. Figure 1(c)

shows an image of a three-dimensional Zn-NM formed on a sapphire substrate, where DEZn molecules were replaced by Zn(acac)<sub>2</sub> molecules based on contrivances (ii) and (iii) [51]. The wavelength of the propagating light for creating the DP was 457 nm. Figure 1 demonstrates that the presented PCVD using the DP is contrary to the common views [b]–[d].

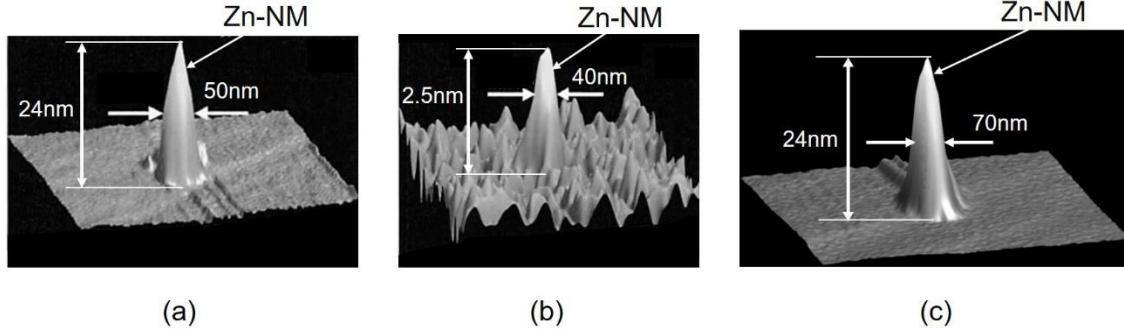


Fig. 1 AFM images of Zn-NMs formed on a sapphire substrate.

Dissociated molecules are DEZn ((a) and (b)) and Zn(acac)<sub>2</sub> (c). The wavelengths of the propagating light for creating the DP were 488nm (a), 684 nm (b), and 457 nm (c).

It should be pointed out that the maximum size  $a_{DP,Max}$  of the DP was estimated from the experimental results of the PCVD above [52]. For this estimation, Fig. 2 was acquired and shows the dependence of the rate  $R$  of depositing Zn atoms on the full-width at the half maximum (FWHM) of the formed Zn-NM. Here, the value of the FWHM increased with increasing deposition time. Closed circles and squares represent the experimental values [53]. The solid curve is the theoretical one fitted to them [54]. This figure shows that the rate  $R$  took the maximum when the FWHM was equal to the tip diameter  $2a_p$  of the fiber probe ( $a_p=4.4$  nm: a tip radius). This was due to the size-dependent resonance of the DP energy transfer between the tip of the fiber probe and the formed Zn-NM (*Phenomenon 4*). Although further increases in the deposition time increased the size of the Zn-NM, the value of  $R$  decreased. Finally, the size and conformation of the Zn-NM reached stationary states, and the value of the FWHM saturated. Figure 1 shows the profiles acquired after this saturation.

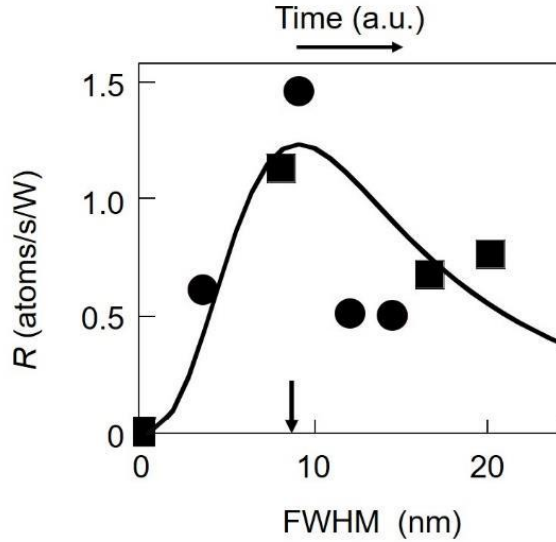


Fig. 2 Dependence of the deposition rate  $R$  (atoms/s/W) on the FWHM of the Zn-NM. FWHM increased with increasing deposition time. The number of atoms deposited per unit time was normalized to the irradiated light power (W) to derive the rate  $R$ . The wavelength of the propagating light for creating the DP was 325 nm. Closed circles and squares represent the measured values when the powers of the light incident to the fiber probe were  $5 \mu\text{W}$  and  $10 \mu\text{W}$ , respectively. The downward arrow represents the value of  $2a_p$ .

It should be noted that the FWHM values in Fig. 1 were 50–70 nm even though the controllability of the tip diameter of the fiber probe was low (contrivance (ii) above). They were independent of the tip diameter, the wavelength and the power of the light used for irradiating the end of the fiber probe, and the species of molecules used. A larger FWHM was not realized even by increasing the deposition time. Here, it should also be noted, based on the Yukawa function mentioned in Section 3.1 and *Phenomenon 4*, that the spatial profile and size of the DP transferred from the tip of the fiber probe corresponded to those of the NM deposited on the substrate. From these results, the values of the FWHM in the AFM images in Fig. 1 indicate the following phenomenon:

*[Phenomenon 9] The maximum size  $a_{DP,Max}$  of the DP is 50–70 nm.*

By using the nano-fabrication technology above, a variety of two-dimensional patterns have been formed by scanning a fiber probe, like a picture drawn with a single stroke of the pen [55]. However, the total scanning time increased with larger pattern sizes, which decreased the working efficiency. To increase the efficiency, a novel lithography technology has been developed in which the fiber probe was replaced by a two-dimensional photo-mask. A small pattern was formed on the material surface by exposing

the thin photoresist film by the DP that was created on the apertures of the photo-mask. For this creation, visible light was used as a light source. Although its wavelength was longer than that of the ultraviolet light required for exposing photoresist in conventional photolithography, it was allowed to be used due to *Phenomenon 8* [56]. Furthermore, an optically inactive photoresist material ZEP-520, popularly used for electron-beam lithography, has been used based on *Phenomenon 5*. A fully automatic practical photolithography machine has been developed and was used to form a diffraction grating pattern with a half-pitch as narrow as 22 nm [57]. It also produced a two-dimensional array of the DP devices reviewed in Section 3.2.1 [58], and practical devices for soft X-rays (a Fresnel zone plate [59] and a diffraction grating [60]).

## (2) Technology not using a fiber probe or an aperture

This part reviews a novel autonomous nano-fabrication technology that requires neither fiber probes nor apertures, resulting in drastic increases in the working efficiency. A representative example is autonomous smoothing of a material surface: The material to be smoothed is installed in a vacuum chamber, and the chamber is also filled with gaseous molecules. By irradiating the material surface with light, the DP is created at the tips of the bumps on the rough material surface. That is, the bumps play the role of a fiber probe for creating the DP. If the molecules jump into the DP field, they are dissociated, as was the case of the PCVD in (1). The chemically active atoms, created as a result of this dissociation, selectively etch the tips of the bumps away, while the flat part of the surface remains unetched. The etching autonomously starts by light irradiation and the surface roughness decreases gradually as etching progresses. The etching autonomously stop when the bumps are annihilated and the DP is not created anymore.

The disc surface of a synthetic silica substrate (30 mm diameter) was etched by using gaseous Cl<sub>2</sub> molecules. Although light with a wavelength shorter than 400 nm was required for conventional photo-dissociation (common view [c]), the present method used visible light with a wavelength of 532 nm based on *Phenomenon 8*. Etching by active Cl atoms decreased the surface roughness to as low as 0.13 nm. A laser mirror was produced by coating a high-reflection film on the smoothed substrate surface, and its damage threshold to the high-power ultraviolet laser light pulses was evaluated. The threshold value was confirmed to be as high as twice that of the commercially available strongest mirror whose substrate surface was polished by a conventional chemical-mechanical polishing technology [61].

Gaseous O<sub>2</sub> molecules can be also used for autonomous etching because the O

atoms created by the dissociation are chemically active. The advantage is that etching can be carried out in atmospheric conditions by using O<sub>2</sub> molecules in air, and thus, a vacuum chamber is not required. Figure 3(a) shows experimental results of etching a plastic PMMA surface by using O<sub>2</sub> molecules [62]. Although ultraviolet light with a wavelength shorter than 242 nm was required for the conventional photo-dissociation, light with a wavelength of 325 nm was used here that was due to *Phenomenon 8*. For comparison, Fig. 3(b) is the result of the etching by using conventional photo-dissociation, for which the wavelength of the light used was as short as 213 nm.

In Figs. 3(a) and (b), the surface roughness was evaluated from its standard deviation  $\sigma(l)$ , by referring to the square root of the variance that has been popularly used for evaluating the frequency fluctuations of microwave oscillators and lasers [63]. The horizontal axis  $l$  represents the period of the roughness on the surface. The vertical axis is the value of  $\sigma(l)$  acquired from the AFM image. Here, the ratio  $\sigma_{after} / \sigma_{before}$  between the values before ( $\sigma_{before}$ ) and after ( $\sigma_{after}$ ) the etching is plotted in a logarithmic scale (This ratio was derived from the values  $\sigma_{before}$  and  $\sigma_{after}$  in Fig. 4 in ref. [62]).

Figure 3(a) shows that  $\sigma_{after} / \sigma_{before} < 1$  in the range  $l < \lambda$  ( $\lambda$  is the wavelength of the light radiated for creating the DP, identified by a downward arrow in this figure), by which the contribution of the sub-wavelength sized DP is confirmed. Drastic decreases in  $\sigma_{after} / \sigma_{before}$  can be seen in the range  $l < 50\text{--}70$  nm, from which *Phenomenon 9* regarding the maximum size of the DP is confirmed again. In contrast to Fig. 3(a), Fig. 3(b) shows that  $\sigma_{after} / \sigma_{before} < 1$  in the range  $l > \lambda$ . This means that the etching was effective in the super-wavelength range. On the contrary,  $\sigma_{after} / \sigma_{before} > 1$  in the sub-wavelength range, which indicates that the surface roughness was increased by the etching. By comparing the two figures, it is confirmed that the etching by the DP is effective for selectively removing bumps of sub-wavelength size.

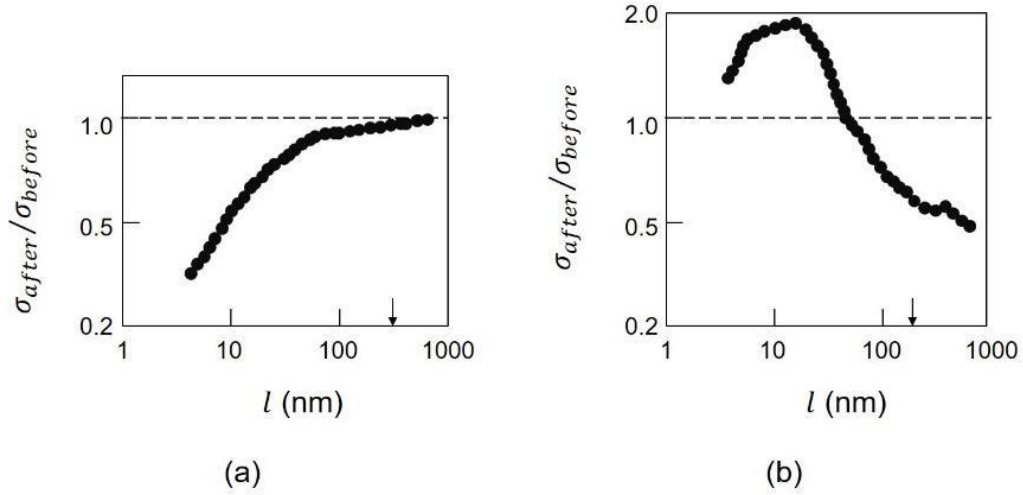


Fig. 3 The ratio of the standard deviation of the roughness of the PMMA surface before and after etching. (a) and (b) are the results acquired by illuminating the surface with light having wavelengths of 325 nm and 213 nm, respectively. The downward arrows represent the values of  $l$  that are equal to the wavelengths above.

Since the DPs are always created on the tip of the bump on the material surface under light irradiation, the present autonomous etching has been applied to a variety of surface profiles. These included a convex surface, a concave surface, and the inner surface of a cylinder. As an example, this etching has smoothed the side surface of a diffraction grating composed of parallel linear corrugated patterns [64] and the surface of a photo-mask used for conventional ultraviolet lithography [65]. Furthermore, a variety of materials have been smoothed, such as the surfaces of GaN crystals [66], transparent ceramics [67], and diamonds [68]. These achievements demonstrated the prominent capability of the present autonomous smoothing technology, achieved by exploiting the DP.

### 3.2.3 Energy conversion

Since the DP field has a broad spectrum, as was described in Section 3.1, the novel phenomena of energy up- and down-conversion are expected. Three kinds of such energy conversions are reviewed in this section.

#### (1) Conversion from optical to optical energy

Energy up-conversion, i.e., the conversion from infrared to visible light, has been realized.



In this process, phonons in the DP provided their energies to the electrons in NMs. NMs of DCM, coumarine 540A, and stilbene 420 dye molecules were used as specimens for demonstrating the up-conversion. By irradiating them with infrared light of 0.8–1.3  $\mu\text{m}$  wavelength, the DP created on one NM was transferred to the adjacent NMs. These NMs received the DP energy that contained the phonon energy, and thus, they respectively emitted red, green, and blue light [69, 70]. This conversion method has been applied to measure infrared optical pulse shapes [71].

Energy down-conversion has also been realized by using an autonomously grown optically curable resin [72] that contains NMs of ZnO and DCM [73]. The DP energy transfer from the ZnO-NM to the DCM-NM and subsequent dissipation, as with the transfer in the nanometer-sized optical devices in Section 3.2.1, realized energy down-conversion: By irradiating the film with ultraviolet light of 300–350 nm wavelength, visible light of 560 nm wavelength was emitted. The conversion efficiency was evaluated to be as high as 90–95 %.

As an application of this down-conversion, a novel plastic film was fabricated by dispersing ZnO and DCM NMs into it [73]. By putting this film on the surface of a commercially available Si solar cell battery (surface area of 156 mm  $\times$  156 mm and nominal electrical power generation efficiency of 18.1 %), the electrical power generation efficiency was evaluated to be 20.0 %. To achieve further increases, another type of film was fabricated by replacing the DCM NMs with BBQ dye NMs. As a result, ultraviolet light of 300–350 nm wavelength was efficiently converted to visible light of 450 nm wavelength. By putting this film on the surface of the Si solar battery above, the electrical power generation efficiency was evaluated to be as high as 20.2 %. It should be pointed out that an efficiency higher than 20% has never been achieved with conventional solitary Si solar batteries.

## (2) Conversion from optical to electrical energy

Novel devices for optical to electrical energy conversion that exhibited the energy up-conversion feature originating from the DP have been fabricated. One example is a photovoltaic device using an organic thin film of P3HT. By depositing Ag nano-particles on the device surface using a novel DP-assisted rf-sputtering method, the conformation of the electrode surface was autonomously controlled [74]. Another example is a Si-photodiode in which the spatial distribution of doped boron (B) atoms was autonomously controlled by a novel DP-assisted annealing [75]. A detailed explanation of this annealing will be given in (3) below. In these two examples, efficient energy up-conversion was

realized even when the incident photon energy was lower than the bandgap energy of the semiconductor materials used for the devices. Furthermore, optical amplification was confirmed, which originated from stimulated emission triggered by the DP.

### (3) Conversion from electrical to optical energy

This part reviews Si light-emitting diodes (LEDs), Si lasers, and SiC polarization rotators as examples of the conversion from electrical to optical energy. Phenomena contrary to the common view [e] are also demonstrated.

Crystalline silicon (Si) has long been a key material supporting the development of modern technology for more than half a century because of its numerous advantages, such as Si's abundance in the earth's crust, and its widespread use for electronics. However, because Si is an indirect-transition-type semiconductor, it has been considered to be unsuitable for light-emitting devices: Since the bottom of the conduction band and the top of the valence band in Si are at different positions in reciprocal lattice space, the momentum conservation law requires an interaction between an electron–hole pair and phonons for radiative recombination. However, the probability of this interaction is very low.

Nevertheless, Si has been the subject of extensive study for the fabrication of light-emitting devices. These include studies using porous Si [76], a super-lattice structure of Si and SiO<sub>2</sub> [77], and so on. However, the devices fabricated in these studies have some limitations, such as low efficiency, the need to operate at low temperature, complicated fabrication processes, and the difficulty of current injection. Experimental work on a novel technology named silicon photonics has recently progressed [78]. Although sophisticated passive optical devices such as optical waveguides and optical switches have been developed, Si light-emitting devices have not been dealt with.

The problems above have been solved by using the DP because the phonons in the DP can provide momenta to the electron to satisfy the momentum conservation law [79]. For fabrication, the DPs were created by irradiating a Si crystal with light, as was the case in the previous parts (1) and (2). For the device operation, DPs were created by electronic excitation, unlike the optical excitations in the case of the previous parts.

#### 1) Infrared Si-LEDs

Fabrication and operation methods are reviewed here by taking an infrared Si-LED as a first example. An n-type Si substrate was used, in which As atoms or Sb atoms were doped. As the first step, the substrate surface was transformed to a p-type material by implanting

B atoms, forming a p-n homojunction. Metallic films were coated on the substrate surfaces to serve as electrodes.

As the next step, this substrate was processed by a novel fabrication method named DP-assisted annealing: By current injection, Joule heat was generated, which caused the B atoms to diffuse. During this Joule-annealing, the substrate surface was irradiated with infrared light (for example, 1.342  $\mu$  m-wavelength light). Because its photon energy  $h\nu_{anneal}$  ( $=0.925\text{eV}$ ) was sufficiently lower than the bandgap energy  $E_g$  ( $=1.12\text{eV}$ ) of Si, the light could penetrate into the Si substrate without suffering absorption. Then, the light reached the p-n homojunction to create the DP on the B atom. The created DP localized at this impurity B atom, which manifested the following phenomenon: [*Phenomenon 10*] *The DP is created and localized at a singularity such as a nanometer-sized particle or impurity atom in a material.*

The phonons in the created DP can provide momenta to the electron nearby to satisfy the momentum conservation law, resulting in radiative recombination for photon emission. This is stimulated emission triggered by the irradiated infrared light. The emitted light propagated out from the crystal to the outside, which indicated that part of the Joule energy used for diffusing the B atoms was dissipated in the form of optical energy, resulting in local cooling that locally decreased the diffusion rate. As a result, by the balance between heating by the Joule energy and cooling by the stimulated emission, the spatial distribution of B atoms varied and reached a stationary state autonomously. This stationary state was expected to be the optimum for efficient creation of the DPs and for efficient LED operation because the probability of spontaneous emission was proportional to that of the stimulated emission described above.

The optimum condition for the DP-assisted annealing has been found based on a two-level system model. That is, the optimum ratio between the irradiated photon number and the injected electron number per unit time was 1:1 [80]. After the DP-assisted annealing, the Huang-Rhys factor, a parameter representing the magnitude of the coupling between electron-hole pairs and phonons, was experimentally evaluated to be 4.08 [81]. This was  $10^2$ – $10^3$  times higher than that before the DP-assisted annealing. It was also found that the DPs coupled with the coherent phonons of the longitudinal optical mode [82].

The device fabricated above was operated as an LED by simple current injection, similar to the case of operating conventional LEDs. By injecting a current of 3.0 A into a device with an areal size of 0.35 mm  $\times$  0.35 mm, a CW output optical power as high as 2.0 W was obtained at a substrate temperature of 77 K. A power as high as 200 mW was

obtained even at room temperature (283 K) [83]. These results confirmed that the following phenomenon occurs: *[Phenomenon 11] The spatial distribution of B atoms varies and reaches a stationary state autonomously due to DP-assisted annealing, resulting in strong light emission from the Si crystal.*

Figure 4 shows the light emission spectra of the fabricated Si-LED acquired at a temperature of 283 K and an injection current of 2.45 A [83]. This figure clearly shows high spectral peaks at  $E_g - 3E_{phonon}$ ,  $E_g - 6E_{phonon}$ , and  $E_g - 9E_{phonon}$  (refer to the arrows A -C), where  $E_{phonon}$  is a phonon energy.

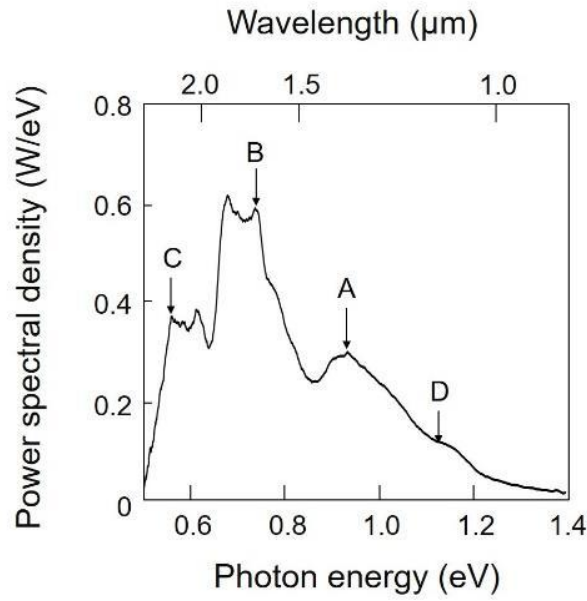


Fig. 4 Light emission spectra of the Si-LED.

The substrate temperature and the injection current were 283 K and 2.45 A, respectively. Downward arrows A – D represent the spectral peaks at  $E_g - 3E_{phonon}$ ,  $E_g - 6E_{phonon}$ ,  $E_g - 9E_{phonon}$ , and  $E_g$ , respectively.

It should be noted that the photon energy emitted from the conventional LEDs was governed by  $E_g$ . However, in the present Si-LED, the energy difference between  $h\nu_{anneal}$  and  $E_g$  was compensated by the created phonon energy. The origin of this

compensation was attributed to the spatial distribution of B atoms that was autonomously controlled during the DP-assisted annealing. For this control, the irradiated light served as a source for creating the DP during the DP-assisted annealing. It has been theoretically confirmed that the DP, after being created and localized on the B atom (*Phenomenon 10*), coupled more efficiently with localized phonons than with non-localized ones. It has been also confirmed that a B atom-pair served as a resonant cavity to confine and localize phonons, resulting in localized phonon creation [84].

For comparing these theoretical confirmations with experimental results, the three-dimensional spatial distribution of B atoms at the p-n homojunction was acquired by atom probe field ion microscopy of sub-nanometer spatial resolution. By analyzing the acquired data, it was found that the B atoms were apt to form pairs with a length  $d = 3a$  ( $a$  (=0.54 nm) is the lattice constant of the Si crystal), and the formed pairs were apt to orient along a plane parallel to the top surface of the Si crystal [85]. That is, the following phenomenon was found: [*Phenomenon 12*] *The length and orientation of the B atom-pair in a Si crystal are autonomously controlled by the DP-assisted annealing.*

It should be noted that the Si crystal is composed of multiple cubic lattices, and the value of the required phonon momentum has to be  $h/a$  for the radiative recombination of the electron (at the bottom of the conduction band at the  $X$ -point in reciprocal space) and the positive hole (at the top of the valence band at the  $\Gamma$ -point) to take place. It should be also noted that the value of the phonon momentum is  $h/3a$  when the phonon localizes at the B atom-pair with  $d = 3a$ . By comparing these values of momenta, it is found that the DP created and localized at this B atom-pair provides three phonons for recombination. As a result, the emitted photon energy  $h\nu_{em}$  is expressed as  $h\nu_{em} = E_g - 3E_{phonon}$ . By substituting the values of  $E_g$  (= 1.12eV) and the relevant optical mode phonon energy  $E_{phonon}$  (=65meV) into this equation, the value of  $h\nu_{em}$  is derived to be 0.93 eV, which is nearly equal to the photon energy  $h\nu_{anneal}$  (=0.95 eV) irradiated during the DP-assisted annealing. This numerical relation is consistent with the spectral feature in Fig. 4. This indicates that the irradiated light served as a breeder that created a photon with energy  $h\nu_{em} = h\nu_{anneal}$  and manifested the following phenomenon: [*Phenomenon 13*] *A light emitting device fabricated by DP-assisted annealing exhibits photon breeding (PB) with respect to photon energy; i.e., the emitted photon energy  $h\nu_{em}$  is equal to the photon energy  $h\nu_{anneal}$  used for the annealing.*

The peaks B and C in this figure are the second and third harmonics of the phonon contributions, respectively. PB was observed also with respect to the photon spin. That is, the polarization direction of the emitted light was identical to that of the light irradiated during the DP-assisted annealing [85].

## 2) Visible LEDs

The second example is visible LEDs fabricated by using crystalline Si and that exhibit the PB phenomenon. Specifically, blue, green, and red light-emitting LEDs were fabricated by radiating blue, green, and red light, respectively, during the DP-assisted annealing [86]. A lateral p-n homojunction structure was developed in order to increase the efficiency of extracting the visible light from the Si crystal [87].

A variety of visible LEDs have been developed by using crystalline SiC even though it is also a well-known indirect transition-type semiconductor. They were fabricated by irradiating them with UV-violet, bluish-white, blue, and green light during the DP-assisted annealing. The fabricated devices emitted UV-violet, bluish-white, blue, and green light, respectively [88].

## 3) Infrared Si-lasers

The third example is high-power infrared Si-lasers. A simple ridge waveguide (10  $\mu\text{m}$ -width and 2  $\mu\text{m}$ -height) was built-in, and the cleaved facets were used as mirrors of a Fabry-Perot cavity (550  $\mu\text{m}$ -cavity length) [89]. DP-assisted annealing was carried out by injecting 1.3  $\mu\text{m}$ -wavelength light into the cavity through one of the end facets. Figures 5(a) and (b) show the light emission spectra of the fabricated device acquired under CW operation at room temperature (25 °C). Above the threshold, a sharp lasing spectrum was observed (Fig. 5(a)), which demonstrated single-mode oscillation even though the cavity length was as long as 550  $\mu\text{m}$ . The origin of this single-mode oscillation was that the low infrared absorption by the Si provided a low threshold for the principal longitudinal mode at the peak of the optical amplification gain spectrum and, as a result, the gains for other modes were depleted by this principal mode due to nonlinear mode competition. The spectral profile below the threshold (Fig.5(b)) does not show any amplified spontaneous emission spectra, which is evidence of gain depletion due to the mode competition above. The lasing wavelength, shown in Fig. 5(a), was 1.271  $\mu\text{m}$ , which was approximately equal to that of the light irradiated during the DP-assisted annealing, from which PB was also confirmed.

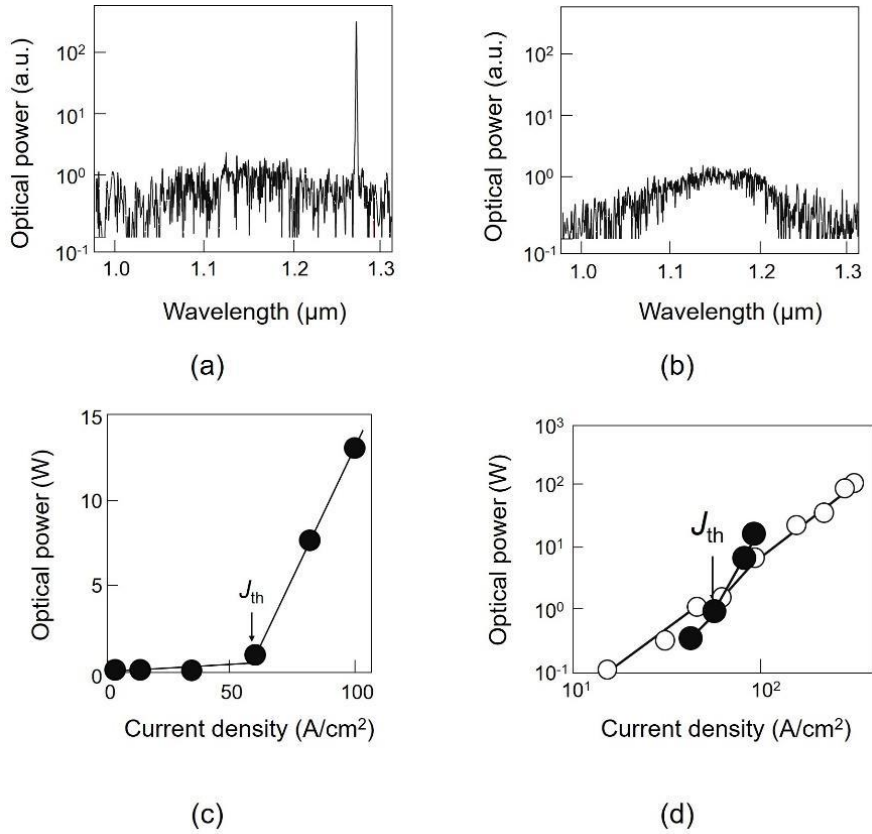


Fig. 5 Light emission spectra and output optical power of Si lasers.

(a), (b) Spectral profiles above and below the threshold, respectively, of a  $550 \mu\text{m}$ -length device with a ridge waveguide. The threshold current density was  $1.1 \text{ A/cm}^2$  under CW operation at room temperature ( $25^\circ\text{C}$ ). (c), (d) Relation between the injected current density and the output optical powers of  $15 \text{ mm}$ -long and  $30 \text{ mm}$ -long devices, respectively.  $J_{th}$  is the threshold current density. Closed circles in (d) are a copy of those in (c).

By modifying the device structure above, high-power infrared laser devices were fabricated. The ridge waveguide was not built into them because further increases in the optical confinement efficiency were not expected in this waveguide as long as the device had a p-n homojunction. Instead, the cavity length was increased to  $15 \text{ mm}$  to realize high-power lasing by utilizing the very low infrared absorption of crystalline Si. Figure 5(c) shows that an output optical power as high as  $13 \text{ W}$  was obtained at the injected current density of  $100 \text{ A/cm}^2$  [90]. The threshold current density  $J_{th}$  was as low as  $60 \text{ A/cm}^2$ . The lasing wavelength was  $1.34 \mu\text{m}$ . As is shown in Fig.5(d), an output optical power higher than  $100 \text{ W}$  was obtained recently by further increases in the cavity length to  $30 \text{ mm}$  [91]. By summarizing the experimental results of the first to the third examples above, the following phenomenon that is contrary to the common view [e] was confirmed:

*[Phenomenon 14] By DP-assisted annealing, a Si crystal works as a high-power light emitting device even though it is an indirect transition-type semiconductor.*

#### 4) Polarization rotators

The last example is polarization rotators fabricated by using a SiC crystal. The fabrication method was equivalent to that of the visible SiC-LEDs of the second example: By implanting Al atoms into an n-type SiC substrate, the substrate surface was transformed to a p-type material, forming a p-n homojunction. By the DP-assisted annealing, during which the substrate surface was irradiated with the 405 nm-wavelength light, diffusion of Al atoms was autonomously controlled to realize the optimum spatial distribution of Al atoms for light emission. As a result, the device worked as a visible LED.

In order to use it as a polarization rotator, an H-shaped electrode was installed on the top surface. By current injection to this electrode, electrons were injected into the p-n homojunction and a magnetic field was generated. It is expected that this current injection rotated the polarization of the light incident into the device. Linearly polarized 405 nm-wavelength light was made normally incident on the top surface of this device. This was because, due to PB, it was also expected that the rotation angle was the largest when its wavelength was identical to that of the light irradiated during the DP-assisted annealing.

Meeting the expectations above, the polarization angle of the incident light actually rotated after propagating through the device. The Verdet constant was evaluated to be 660 deg/A from the measured values of the polarization rotation angle. This is  $10^5$ - $10^6$  times those of conventional paramagnetic materials that are transparent in the visible region. The Faraday rotation angle was also as large as 2480 deg/cm. These large values demonstrated that the present SiC crystal exhibited a gigantic magneto-optical effect. Furthermore, the remanent magnetization was 0.36 mT, which corresponded to those in conventional ferromagnetic materials [92]. The experimental results above indicated that the presently used SiC crystal acquired novel properties, equivalent to those of ferromagnetic materials.

In order to find the origin of such novel ferromagnetic properties, a magnetization curve was acquired at 27 °C. Closed squares in Fig. 6 are the acquired values. They were fitted by the curve A and clearly exhibited a hysteresis characteristic, which is inherent to ferromagnetic materials. The values of the magnetization were very small before the DP-assisted annealing, as shown by open circles and the curve B. By comparing these measured values, the following novel phenomenon was confirmed: *[Phenomenon 15] The semiconductor SiC crystal was made to behave as a ferromagnet as a result of the DP-assisted annealing and exhibited a gigantic magneto-optical effect*



in the visible region.

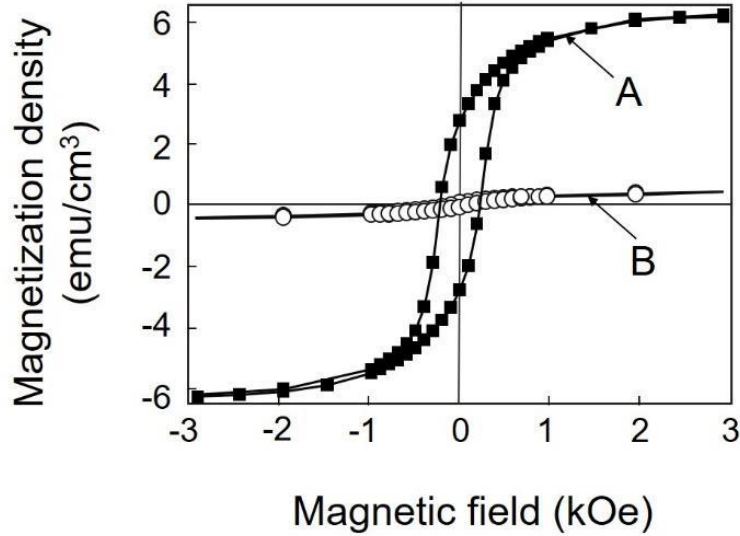


Fig.6 Magnetization curve for the SiC crystals, measured at 27 °C.

Closed squares and open circles are the results acquired after and before the DP-assisted annealing, respectively. They are fitted by the curves A and B, respectively.

The origin of this behavior has been attributed to the Al atom-pairs that were autonomously formed as a result of the DP-assisted annealing. That is, the ferromagnetic characteristic likely originated from the two electrons with parallel spins in the triplet state of the electron orbital in an Al atom-pair, which was more stable than the singlet state.

At the end of this part it should be pointed out that similar polarization rotators have also been fabricated by using ZnO crystals based on the same principle as in the SiC crystals above [93].

#### 4 Future Directions

The studies reviewed in Section 3 identified the DP as a quantum field that is created as a result of the light-matter interaction in a nanometer-sized space. However, they also presented at least two theoretical difficulties. One was that the mode of the electromagnetic field could not be defined. The other was that the description of the spatial localization of the DP required the surrounding macroscopic subsystem to have a parabolic dispersion relation. As an urgent solution to overcome these difficulties, the

theoretical methods in on-shell science were modified and applied to tentatively describe the physical nature of the DP, as was reviewed in Section 3.1.

Although the theoretical studies above were at a standstill, experimental studies have found the novel *Phenomena 1-15* described in Section 3. It should be noted that they cannot be described by conventional optical theories. This is because these theories treat only photons in a vacuum (free photons) and in a macroscopic material, whose dispersion relation is given by the mass-shell (“on-shell” for short). It has been popularly known that massless particles with non-zero spin, such as free photons, cannot be localized in space in the sense that the position operator cannot be defined [94]. However, it turns out to be natural to consider localized photons when the effective mass of photons, created by light–matter interactions, is taken into account. Especially in the case of NMs, space–time localization and energy–momentum fluctuations constitute novel aspects of light. A photon in such a context is called a DP.

For a theoretical definition of the DP and for describing the *Phenomena 1-15* above, the “off-shell” nature of the interaction has to be considered. That is, the DP is an off-shell quantum field that conspicuously deviates from the mass-shell. As has been well known, quantum field theories cannot be formulated without off-shell entities. In other words, the traditional particle description has failed to treat the quantum field of a composite system. Hence, DPs must be entities that are very different from Einstein’s quanta of light or free photons.

Here, a fundamental question arises: How can the DP be described as an individual entity? As long as one sticks to the notion of individual entities as irreducible on-shell particles, it is impossible to treat the DP as an individual entity. However, a more general perspective, advocated by Ojima [95], has shown that macroscopic physical phenomena can emerge out of a condensation of microscopic off-shell entities.

By following this perspective, a basic idea can be proposed: In the interaction between light and NMs, certain families of modes of the composite system will behave as individuals. This behavior suggests that the DP is the quantum field of a composite system in which an electromagnetic field and an electron (or an exciton) interact in a nanometer-sized space. Furthermore, it is a virtual field localized in the nanometer-sized space within a short time duration. Thus, the DP is a quantum field whose nature is contrary to that of an on-shell photon. This means that conventional optical theories are incapable of giving a systematic description of *Phenomena 1-15*. Fortunately, however, several hints have been given to construct novel theories for describing the phenomena above by noting that the virtual photon plays an essential role in the electromagnetic Coulomb interactions. They are:

[A] The longitudinal mode of an electromagnetic field (the longitudinal wave) contributes to the Coulomb interaction [96].

[B] The field interaction accompanies the 4-momentum [97].

[C] Although the spacelike field is not spatially localized because it behaves as a stable wave, it becomes unstable and can localize if it interacts with a timelike field [98].

By referring to these hints, novel theoretical studies have commenced by relying on physical bases [99]. One is the theory using electromagnetic response functions based on classical electromagnetics. The other is the theory based on spatio-temporal vortex hydrodynamics supported by the relativity theory [100].

Furthermore, mathematics-based theoretical studies are in progress that will serve as invaluable guides for gaining a deep understanding of the concepts of the physics-based theories for the phenomena that originate from the DP [99]. Examples of these theories are the quantum probability theory and the quantum measurement theory. Also demonstrated is a theory based on micro–macro duality, which serves as a foundation for embarking on theoretical studies of off-shell science.

One of the promising future direction of DP science is to propel the theoretical studies above in collaboration with experimental ones. By using the fruits of these studies, further developments of application technologies are expected, resulting in further disruptive innovations.

## 5 Summary

This paper reviewed the progress in optical sciences dealing with the ONF. After the introduction in Section 1, the first half of Section 2 pointed out that the ONF was an electromagnetic field that is created and localized in an NM, or on its surface, under light illumination.

The second half of Section 2 reviewed the classical studies of the ONF that explored the possibilities of creating and using the ONF. It described that the studies on the ONF, called the near field optics, started for realizing disruptive innovation by breaking through the diffraction limit of optical microscopy. Its methodology was proposed in the 1920s to 1950s, and experimental demonstrations were carried out in the 1980s and 1990s. It was pointed out that the classical studies of the ONF had already come to an end without answering the essential questions on the origin of the near-field optical interaction.

However, even after this end, basic studies on the ONF were steadily continued by a small number of scientists. These included studies on the concepts and principles of

the ONF, with the aim of answering the questions above. As a result, as was reviewed in Section 3.1, the ONF was identified as an off-shell quantum field, i.e., a virtual field localized in a nanometer-sized space within a short time duration. Based on this identification, a novel off-shell science has started by noting that the dispersion relation between the energy and momentum was invalid for the ONF. This quantum field is now called the DP because it is created as a result of the interaction between photons and electrons (or excitons) in a NM, and thus, it accompanies the energies of electrons or excitons. In the other words, the DP is a quantum field created in a system composed of electromagnetic fields and NMs.

Sections 3.2 and 3.3 reviewed novel *Phenomena 1-15* that have been found in a series of experimental studies on the DP. They are contrary to the common views that have been accepted for a long time by conventional optical science. By applying these phenomena, a variety of technologies have been developed. These include nanometer-sized optical devices (including their applications to information transmission and processing systems), nano-fabrication technology (photochemical vapor deposition, lithography, and smoothing of material surfaces), and three kinds of energy conversion technologies. Among these energy conversion technologies, the electrical to optical energy conversion used a DP that was created as a result of electrical excitation by current injection. This conversion realized high-power light emitting diodes and lasers by using crystalline Si, which is a typical indirect-transition-type semiconductor. A polarization rotator was realized by using crystalline SiC (also an indirect-transition-type semiconductor) that exhibited a gigantic magneto-optical effect.

Section 4 reviewed the advent of novel theories. These included a theory using electromagnetic response functions, a theory based on spatio-temporal vortex hydrodynamics supported by relativity theory, quantum probability theory, quantum measurement theory, and a theory based on micro–macro duality.

## References

1. Ohtsu, M.(ed.) in Near-Field Nano/Atom Optics and Technology Ch.1 (Springer Tokyo, 1998).
2. Zhu, X and Ohtsu, M. in Near-Field Optics: Principles and Applications, Ch.1 (World Scientific, 2000).
3. Ohtsu, M. From Classical to Modern Near-Field Optics and the Future. *Opt. Rev.*, **21**, 905-910 (2014).
4. Synge, E.H. A Suggested Method for Extending Microscopic Resolution into the Ultra-Microscopic Region. *Phil. Mag.*, **6**, 356-362 (1928).
5. Aloysuis, J. Resolving power of visible light. *Journal of the Optical Society of America*, **46**, 359 (1956).
6. Bethe, H. Theory of diffractin by small holes. *Phys. Rev.*, **66**, 163-182 (1944).

7. Bouwkamp, C.J. On the Diffraction of Electro-Magnetic Waves by Small Circular Discs and Holes. *Philips Res. Rep.*, **5**, 401-422 (1950).
8. Ash, E. A. & Nicholls, G. Super-Resolution Aperture Scanning Microscope. *Nature*, **237**, 510-516 (1972).
9. Pohl, D.W. & Courjon, D. (ed.) Near Field Optics (Kluwer, 1993).
10. Pohl, D.W., Denk, W. & Lanz, M. Optical stethoscopy: Image recording with resolution  $\lambda/20$ . *Applied Physics Letters*, **44**, 651-653 (1984).
11. Lewis, A., Isaacson, M., Harootunian, A. & Muray, A. Development of a 500 Å spatial resolution light microscope. I. Light is efficiently transmitted through  $\lambda/16$  diameter apertures. *Ultramicroscopy*, **12**, 227-231 (1984).
12. Fischer, U.Ch. Optical characteristics of 0.1  $\mu\text{m}$  circular apertures in a metal film as light sources for scanning ultramicroscopy. *Journal of Vacuum Science & Technology B*, **3**, 386-390 (1985).
13. Betzig, E., Isaacson, M. & Lewis, A. Collection mode near-field scanning optical microscopy. *Applied Physics Letters*, **51**, 2088-2090 (1987).
14. Mononobe, S. & Saiki, T. in Near-Field Nano/Atom Optics and Technol.(ed Ohtsu, M.) ( Springer Tokyo, 1998) Chs.3 and 4.
15. Betzig, E., Trautman, J.K., Harris, T.D., Weiner, J.S. & Kostelack, R.L. Breaking the Diffraction Barrier: Optical Microscopy on a Nanometric Scale. *Science*, **251**, 1468-1470 (1991).
16. Pangaribuan, T., Yamada, K., Jian, S., Ohasawa, H. & Ohtsu, M. Reproducible fabrication technique of nanometric tip diameter fiber probe for photon scanning tunneling microscope. *Japanese Journal of Applied Physics*, **31**, L1302-L1304 (1992).
17. Malmqvist, L. & Hertz, H.M. Trapped particle optical microscopy. *Optics Communications*, **94**, 19-24 (1992).
18. Van Hulst, N.F. et al. Near-field optical microscope using a silicon-nitride probe. *Applied Physics Letters*, **62**, 461-463 (1993).
19. Zenhausern, F., Martin, Y. & Wickramasinghe, H.K. Scanning Interferometric Apertureless Microscopy: Optical Imaging at 10 Angstrom Resolution. *Science*, **269**, 1083-1085 (1995).
20. Guerra, J.M. Photon tunneling microscopy. *Applied Optics*, **29**, 3741-3752 (1990).
21. Betzig, E. & Chichester, R.J. Single Molecules Observed by Near-Field Scanning Optical Microscopy. *Science*, **262**, 1422-1425 (1986).
22. Xie, X.S. & Dunn, R.C. Probing Single Molecule Dynamics. *Science*, **265**, 361-364 (1994).
23. Maheswari, R.U., Mononobe, S., Tatsumi, H., Katayama, Y. & Ohtsu, M. Observation of Subcellular Structures of Neurons by an Illumination Mode Near-Field Optical Microscope under an Optical Feedback Control. *Optical Review*, **3**, 463-467 (1996).
24. Levy, J., Nikitin, V., Kikkawa, J.M., Awschalom, D.D. & Samarth, N. Femtosecond near-field spin microscopy in digital magnetic heterostructures. *Journal of Applied Physics*, **79**, 6095-6100 (1996).

25. Saiki, T., Nishi, K. & Ohtsu, M. Low temperature near-field photoluminescence spectroscopy of InGaAs single quantum dots. *Jpn. J. Appl. Phys.*, **37**, 1638-1642 (1998).
26. Narita, Y. & Murotani, H. Submicrometer optical characterization of the grain boundary of optically active Cr<sup>3+</sup> doped polycrystalline Al<sub>2</sub>O<sub>3</sub> by near-field spectroscopy. *American Mineralogist*. **87**, 1144-1147 (2002).
27. Isaacs, M., Cline, J. & Barshatzky, H. Resolution in near-field optical microscopy. *Ultramicroscopy*, **47**, 15-22 (1992).
28. Wolf, E. & Nieto-Vesparinas, M. Analyticity of the angular spectrum amplitude of scattered fields and some of its consequences. *Journal of the Optical Society of America*, **2**, 886-890 (1985).
29. Girard, C. & Courjon, D. Model for scanning tunneling optical microscopy: A microscopic self-consistent approach. *Phys. Rev.*, **B 42**, 9340-9439 (1990).
30. Eah, S.-K., Jhe, W., Saiki, T. & Ohtsu, M. Study of Quantum Optical Effects with Scanning Near-Field Optical Microscopy, *The First Asia-Pacific Workshop on Near Field Optics*, abstr. 25 (1996).
31. Kobayashi, K. & Ohtsu, M. Quantum theoretical approach to a near-field optical system. *Journal of Microscopy*, **194**, 249-254 (1999).
32. Kobayashi, K., Sangu, S., Ito, H. & Ohtsu, M. Near-field optical potential for a neutral atom. *Physical Review A*, **63**, 1-9 (2001).
33. Ito, H., Nakata, T., Sakaki, K. & Ohtsu, M. Laser Spectroscopy of Atoms Guided by Evanescent Waves in Micron-Sized Hollow Optical Fibers. *Physical Review Letters*, **76**, 4500-4503 (1996).
34. Ohtsu, M., Kobayashi, K., Kawazoe, T., Sangu, S. & Yatsui, T. Nanophotonics: "Design, Fabrication, and Operation of Nanometric Devices Using Optical Near Fields. *IEEE J. of Selected Topics in Quantum Electron.*, **8**, 839-862 (2002).
35. Ohtsu, M. (ed.) Handbook of Nano-Optics and Nanophotonics (Springer, 2013).
36. Ohtsu, M. in Progress in Nanophotonics 4 (ed. Yatsui, T.) Ch.1 (Springer, 2018).
37. Tanaka, Y. & Kobayashi, K. Spatial localization of an optical near field in one-dimensional nanomaterial system. *Physica*, **E 40**, 297-300 (2007).
38. Sangu, S., Kobayashi, K. & Ohtsu, M. Optical near fields as photon-matter interacting systems. *J. Microscopy*, **202**, 279-285 (2001).
39. Maier, S.A. et al. Plasmonics-A route to nanoscale optical devices. *Advanced Materials*, **13**, 1501-1505 (2001).
40. Sangu, S., Kobayashi, K., Shojiguchi, S. & Ohtsu, M. Logic and functional operations using a near-field coupled quantum-dot system. *Phys. B*, **69**, 115334 (2004).
41. Kawazoe, T. et al. Two-dimensional array of room-temperature nanophotonic logic gates using InAs quantum dots in mesa structures. *Appl. Phys. B*, **103**, 537-546 (2011).
42. Kawazoe, T., Tanaka, S. & Ohtsu, M. A single-photon emitter using excitation energy transfer between quantum dots. *J. Nanophoton.* **2**, 029502 (2008).

43. Naruse, M. et al. Energy dissipation in energy transfer mediated by optical near-field interactions and their interfaces with optical far-fields. *Appl. Phys. Lett.*, **100**, 241102 (2012).
44. Naruse, M. et al. Autonomy in excitation transfer via optical near-field interactions and its implications for information networking. *Nano Communication Networks*, **2**, 189-195 (2011).
45. Naruse, M., Tate, N., Aono, M. & Ohtsu, M. Information physics fundamentals of nanophotonics. *Rep. Prog. Phys.*, **76**, 056401 (2013).
46. Kim, S.-J., Naruse, M., Aono, M., Ohtsu, M. & Hara, M. Decision Maker based on Nanoscale Photoexcitation Transfer. *Scientific Report*, **3**, 2370 (2013).
47. Aono, M. et al. Amoeba-Inspired Nanoarchitectonic Computing: Solving Intractable Computational Problems Using Nanoscale Photoexcitation Transfer Dynamics. *Langmuir*, **29**, 7557-7564 (2013).
48. Tate, N. et al. Quadrupole-Dipole Transform based on Optical Near-Field Interactions in Engineered Nanostructures. *Optics Express*, **17**, 11113-11121 (2009).
49. Tate, N. et al. Nanophotonic code embedded in embossed hologram for hierarchical information retrieval. *Optics Express*, **18**, 7497-7505 (2010).
50. Kawazoe, T., Kobayashi, K., Takubo, S. & Ohtsu, M. Nonadiabatic photodissociation process using an optical near field, *J. Chem. Phys.* **122**, 024715 (2005).
51. T. Kawazoe, K. Kobayashi, and M. Ohtsu, Near-field optical chemical vapor deposition using Zn(acac)<sub>2</sub> with a non-adiabatic photochemical process, *Appl. Phys. B*, **84**, 247-251 (2006).
52. Ohtsu, M., & Kawazoe, T., Experimental estimation of the maximum size of a dressed photon. Preprint at <http://offshell.rodrep.org/?p=98> (2018) DOI: 10.14939/1802R.001.v1.
53. Lim, J. , Yatsui, T. & Ohtsu, M. Observation of Size-Dependent Resonance of Near-Field Coupling between a Deposited Zn Dot and the Probe Apex during Near-Field Optical Chemical Vapor deposition. *IEICE Trans. Electron.*, **E88-C** ,1832-1834 (2005).
54. Sangu, S. Kobayashi, K. & Ohtsu, M. Optical near fields as photon-matter interacting systems. *J. Microscopy*, **202**, 279-285 (2001).
55. Polonski, V. V., Yamamoto, Y., Kouroggi, M., Fukuda, H. & Ohtsu, M. Nanometric patterning of zinc by optical near-field photochemical vapour deposition. *J. Microscopy*, **194**, 545-551 (1999).
56. Yonemitsu, H., Kawazoe, T., Kobayashi, K. & Ohtsu, M. Nonadiabatic photochemical reaction and application to photolithography, *Journal of Photoluminescence*, **122-123**, 230-233 (2007).
57. Inao, Y., Nakasato, S., Kuroda, R. & Ohtsu, M. Near-field lithography as prototype nano-fabrication tool, *Microelectronic Engineering*, **84**, 705-710 (2007).
58. Kawazoe, T. et al. Demonstration of nanophotonic NOT gate using near-field optically coupled quantum dots. *Applied Physics B*, **84**, 243–246 (2006).
59. Kawazoe, T. , Takahashi T. & Ohtsu, M. Evaluation of the dynamic range and spatial resolution of nonadiabatic optical near-field lithography through fabrication of Fresnel zone plates. *Appl. Phys. B*, **98**, 5-11 (2010).

60. Koike, M., Miyauchi, S., Sano, K. & Imazono, T. in Nanophotonics and Nanofabrication, (ed. Ohtsu, M.), Ch.9 (Wiley-VCH, 2009).
61. Hirata, K. Realization of high-performance optical element by optical near-field etching, *Proc. SPIE* **7921**, 79210M (2011).
62. Yatsui, T., Nomura, W & M. Ohtsu. Realization of Ultraflat Plastic Film using Dressed-Photon–Phonon-Assisted Selective Etching of Nanoscale Structures, *Advances in Optical Technologies*, **2015**, 701802 (2015).
63. Allan, D.W. Statistics of Atomic Frequency Standards, *Proc. IEEE*, **54**, pp.221-230 (1966).
64. Yatsui, T. et al. Self-organized near-field etching of the sidewalls of glass corrugations. *Appl. Phys. B* **103**, 527-530 (2011).
65. Teki, R. et al. Alternative smoothing techniques to mitigate EUV substrate defectivity. **Proc. SPIE** **8322** (2012) 83220B.
66. Yatsui, T. et al. Challenges in realizing ultraflat materials surfaces. *Beilstein J. Nanotechnol.* **4**, 875-885 (2013).
67. Nomura, W. et al. Repairing nanoscale scratched grooves on polycrystalline ceramics using optical near-field assisted sputtering. *Appl. Phys. B*, **99**, 75-78 (2010).
68. Yatsui, T. Nomura, W. M. Naruse & Ohtsu, M. Realization of an atomically flat surface of diamond using dressed photon-phonon etching. *J. Phys. D*, **45**, 475302 (2012).
69. Kawazoe, T., Fujiwara, H., Kobayashi, K. & Ohtsu, M. Visible light emission from dye molecular grains via infrared excitation based on the nonadiabatic transition induced by the optical near field. *Journal of Selected Topics in Quantum Electronics*, **15**, 1380-1386 (2009).
70. Fujiwara, H., Kawazoe, T. & Ohtsu, M. Nonadiabatic multi-step excitation for the blue–green light emission from dye grains induced by the near-infrared optical near-field. *Appl. Phys. B*, **98**, 283-289 (2010).
71. Fujiwara, H., Kawazoe, T. & Ohtsu, M. Nonadiabatic nondegenerate excitation by optical near-field and its application to optical pulse-shape measurement. *Appl. Phys. B*, **100**, 85-91 (2010)..
72. Tate, N. et al. Experimental demonstration and stochastic modeling of autonomous formation of nanophotonic droplets. *Appl. Phys. B*, **112**, 587-592 (2013).
73. Ohtsu, M. in Progress in Nanophotonics, Vol.5 (ed. Yatsui, T.) Ch.1 (Springer, 2018).
74. Yukutake, S. et al. Selective photocurrent generation in the transparent wavelength range of a semiconductor photovoltaic device using a phonon-assisted optical near-field process. *Appl. Phys. B*, **99**, 415-422 (2010).
75. Tanaka, H., Kawazoe, T. & Ohtsu, M. Increasing Si photodetector photosensitivity in near-infrared region and manifestation of optical amplification by dressed photons. *Appl. Phys. B*, **108**, 51-56 (2012).
76. Hirschman, K.D., Tysbekov, L., Duttagupta, S.P., & Fauchet, P.M. Silicon-based visible light emitting



- devices integrated into microelectronic circuits. *Nature*, **384**, 338-341 (1996). DOI:10.1038/384338a0
77. Lu, Z.H., Lockwood, D.J., and Baribeau, J.M. Quantum confinement and light emission in SiO<sub>2</sub>/Si superlattices. *Nature*, **378**, 258–260 (1995). DOI: 10.1038/378258a0
  78. Milosevic, M.M. et al. Ion Implantation in Silicon for Trimming the Operating Wavelength of Ring Resonators. *IEEE J. Sel. Top. Quant.*, **24**, 8200107 (20189). DOI: 10.1109/JSTQE.2018.2799660
  79. Kawazoe, T., Mueed, M.A. & Ohtsu, M. Highly efficient and broadband Si homojunction structured near-infrared light emitting diodes based on the phonon-assisted optical near-field process, *Appl. Phys. B*, **104**, 747-754 (2011).
  80. Kim, J.H., Kawazoe, T. & Ohtsu, M. Optimization of dressed-photon—phonon-assisted annealing for fabricating GaP light-emitting diodes. *Applied Physics A*, **121**, 1395-1401 (2015).
  81. Yamaguchi, M., Kawazoe, T. & Ohtsu, M. Evaluating the coupling strength of electron–hole pairs and phonons in a 0.9 μm-wavelength silicon light emitting diode using dressed-photon–phonons. *Appl. Phys. A*, **115**, 119-125 (2013).
  82. Wada, N., Tran, M.-A., Kawazoe, T. & Ohtsu, M. Measurement of multimode coherent phonons in nanometrics spaces in a homojunction-structured silicon light emitting diode. *Appl. Phys. A*, **115**, Issue 1, April 2014, pp. 113-118 (2014).
  83. Ohtsu, M. & Kawazoe, T. Principles and practices of Si light emitting diodes using dressed photons. *Adv. Mat. Letters*, **10**, pp.860-867 (2019).
  84. Tanaka, Y. & Kobayashi, K. Optical near field dressed by localized and coherent phonons. *J. Microscopy*, **229**, 228-232 (2007).
  85. Kawazoe, T., Nishioka, K., & Ohtsu, M. Polarization control of an infrared silicon light-emitting diode by dressed photons and analyses of the spatial distribution of doped boron atoms. *Applied Physics A*, **121**, 1409-1415 (2015).
  86. Tran, M. A., Kawazoe, T. & Ohtsu, M. Fabrication of a bulk silicon p-n homojunction-structured light emitting diode showing visible electroluminescence at room temperature. *Appl. Phys. A*, **115**, 105-111 (2014).
  87. Yamaguchi, M., Kawazoe, T., Yatsui, T. & Ohtsu, M.: Spectral properties of a lateral p-n homojunction-structured visible silicon light-emitting diode fabricated by dressed-photon—phonon-assisted annealing. *Appl. Phys. A*, **121**, 1389-1394 (2015).
  88. Ohtsu, M. in *Silicon Light-Emitting Diodes and Lasers*. Ch.6 (Springer, 2016) Ch. 6.
  89. Kawazoe, T., Ohtsu, M., Akahane, K. & Yamamoto, N. Si homojunction structured near-infrared laser based on a phonon-assisted process. *Appl. Phys. B*, **107**, 659-663 (2012).
  90. Kawazoe, T. High power Silicon laser based on the dressed photon technology. Extended Abstracts of the 2017 International Conference on Solid State Devices and Materials, paper number H-7-0, 413-414 (2017).
  91. Ohtsu, M., Ojima, I. & Sakuma, H. in *Progress in Optics Vol.62* (ed. Visser, T. ) Ch. 1 (Elsevier, 2019)

- (in the press).
92. Ohtsu, M. in *Silicon Light-Emitting Diodes and Lasers*. Ch.6 (Springer, 2016) Ch. 8.
  93. Tate, N., Kawazoe, T., Nomura, W. & Ohtsu, M. Current-induced giant polarization rotation using ZnO single crystal doped with nitrogen ions. *Sci. Reports*, DOI 10.1038/srep12762, August 2015
  94. Newton, T.D. & Wigner, E. P. Localized States for Elementary Systems. *Rev. Mod. Phys.*, **21**, 400-406 (1949).
  95. Ojima, I. Micro-macro duality in quantum physics. in *Stochastic Analysis: Classical and Quantum Perspectives of White Noise Theory*, (ed. T. Hida) Ch.12 (World Scientific, 2005).
  96. Ojima, I. Nakanishi-Lautrup,  $\mathbb{B}$  field, crossed product and duality. *Research on Quantum Field Theory, RIMS Workshop*, abstr.29 (2006).
  97. Del'Antonio, G.F. Support of a field in  $p$  space. *J. Math. Phys.* **2**, 759-766 (1961).
  98. Aharanov, Y., Komar, A. & Susskind, L. Superluminal Behavior, Causality, and Instability. *Phys. Rev.* **182**, 1400-1403 (1969).
  99. Yatsui, T. (ed). *Progress in Nanophotonics*, Vol.5 (Springer, 2018).
  100. Ohtsu, M., Ojima, I. & Sakuma, H. in *Progress in Optics*, Vol.64 (ed. Visser, T.D.) Chapter 2 (Elsevier, 2019).